

Baryon asymmetry of the Universe and CP violation

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PCPV, Mahabaleshwar, 21 Feb 2013

Overview

- Three paradigms of baryogenesis :
 - GUT decay ... essentially thermal
 - TeV scale ... essentially non-thermal
 - Leptogenesis ... both possibilities
- Sphaleron physics
 - MSSM status
- Leptogenesis – the thermal case
 - ... very constrained
 - relation to light neutrino data
- Leptogenesis – the non-thermal case
 - ... lack of quantitative constraints
 - robust relation to spontaneous parity violation
- Some observational possibilities
 - Gravitational waves from bubble wall decays

Current status

From Nucleosynthesis calculations and
observed abundances of D, ^3He , ^4He and ^7Li ,

$$\eta \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} \simeq 5 \times 10^{-10}; \quad 0.017 < \Omega_B h^2 < 0.024$$
$$H_0 \equiv h 100 \text{ km/s/Mpc}; \quad h \simeq 0.7$$

Note from random fluctuations at the QCD scale, the residual η would be 10^{-17}

From WMAP data,

$$\Omega_B h^2 \simeq 0.022$$

Genesis of baryogenesis

- CP violation discovery 1964
- CMBR discovery also 1965 ...
- The possibility of *explaining* baryon asymmetry

$$\frac{n_B}{s} \simeq 10^{-9}$$

- Weinberg Brandeis lectures 1965; esp. Sakharov 1967 proposes :

GUT scale baryogenesis

(Sakharov 1967; Yoshimura; Weinberg 1978)

1. There should exist baryon number B violating interaction

$$\begin{array}{ll} X \rightarrow qq & \Delta B_1 = \frac{2}{3} \\ & \bar{q}\bar{l} \quad \Delta B_2 = -\frac{1}{3} \end{array}$$

2. Charge conjugation C must be violated

$$\mathcal{M}(X \rightarrow qq) \neq \mathcal{M}(\bar{X} \rightarrow \bar{q}\bar{q})$$

3. CP violation

$$r_1 = \frac{\Gamma(X \rightarrow qq)}{\Gamma_1 + \Gamma_2} \neq \frac{\bar{\Gamma}(\bar{X} \rightarrow \bar{q}\bar{q})}{\bar{\Gamma}_1 + \bar{\Gamma}_2} = \bar{r}_1$$

4. Out of equilibrium conditions

Reverse reactions don't get the time to reverse the products

Net baryon asymmetry

$$\begin{aligned} B &= \Delta B_1 r_1 && + \Delta B_2 (1 - r_1) \\ &+ (-\Delta B_1) \bar{r}_1 && + (-\Delta B_2) (1 - \bar{r}_1) \\ &= (\Delta B_1 - \Delta B_2) (r_1 - \bar{r}_1) \end{aligned}$$

- GUTs generically involve new gauge forces which mediate B violation
- Higgs scalar interactions can be natural source of CP violation
- The Particle Physics rates and expansion rate of the Universe compete

$$\Gamma_x \cong \alpha_x m_x^2 / T; \quad H \cong g_*^{1/2} T^2 / M_{\text{Pl}}$$

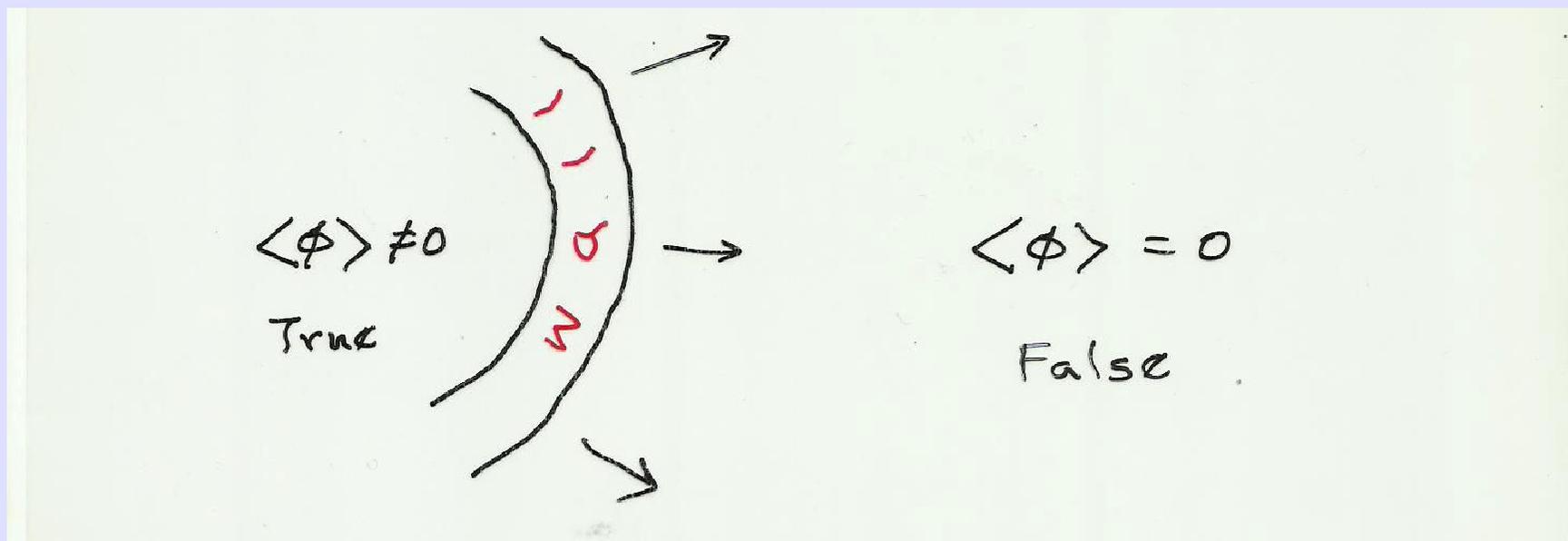
However, rather startling additional inputs appear from global aspects of SM gauge group.

TeV scale baryogenesis

- B and L are known to be accidental symmetries of SM at tree level
- $B + L$ turns out to be anomalous

$$\text{Tr}(T^a \{\tau^b, \tau^c\}) \neq 0$$

- Anomalous processes are suppressed at $T = 0$; unsuppressed for $T \gg M_W$
- Two conclusions :
 - Any $B + L$ generated at high scale will be erased
 - ... there is a way to violate $B + L$ just as we cool below M_W
- Expansion rate H too slow at electroweak scale – need another source of out of equilibrium conditions \rightarrow **First Order Phase Transition** (FOPT)
- First order phase transition in SM requires Higgs mass to be $\lesssim 90\text{GeV}$



- Thick wall, slow bubbles : scalar condensate with transient CP phase; sphalerons fit in the wall
- Thin wall, fast bubbles : CP phase as before, fermions scatter from the walls

In either case we need to go beyond the SM :

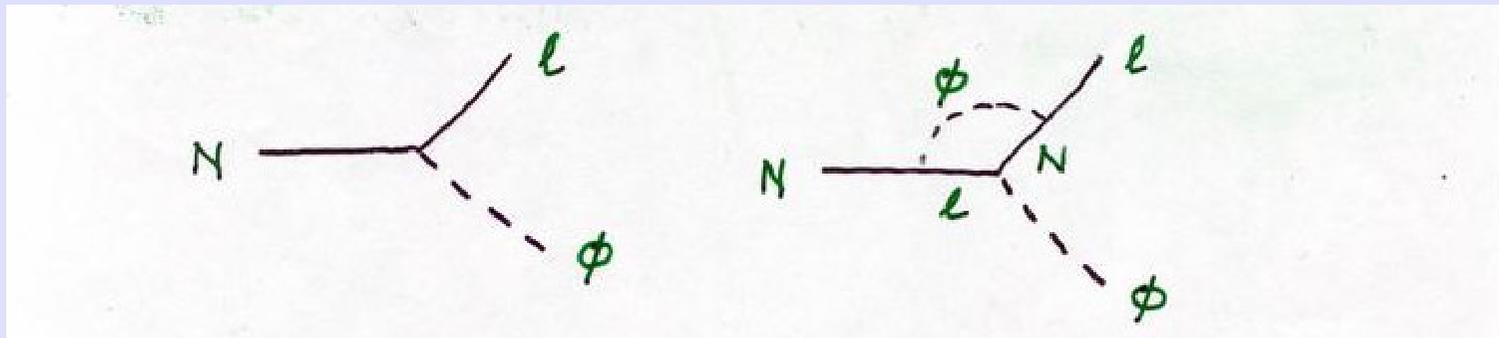
- CKM phase acquired at the wall; but magnitude too small
- At least two scalars as order parameters of the phase transition. Minimal model : 2 Higgs Doublets

→ MSSM as realistic and adequate (summary later)

Leptogenesis

(Fukugita and Yanagida 1986)

- Out of equilibrium decay of heavy Majorana neutrinos

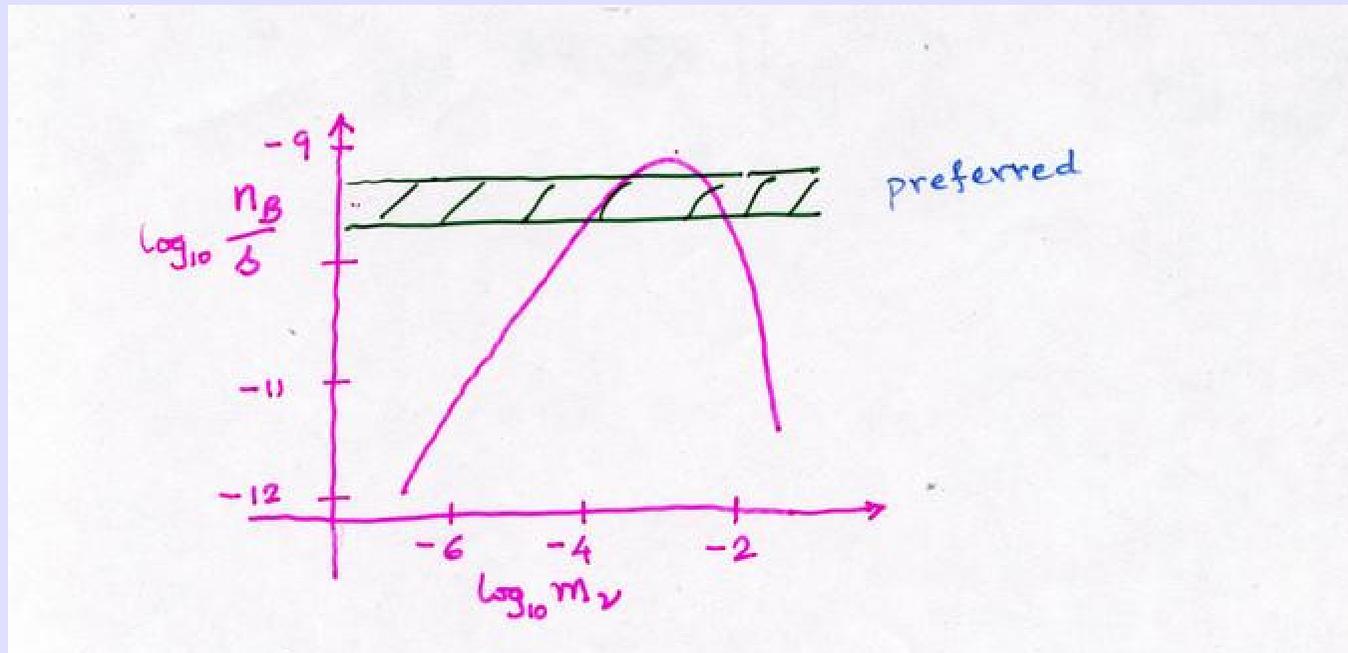


- Easy to arrange CP violation due to complex vacuum expectation values of scalar fields producing the mass

$$\frac{r - \bar{r}}{r} \sim \frac{1}{v^2 m_D^2} \text{Im}(m_D^\dagger m_D)^2$$

- Need to have comparable, faster, expansion rate of the Universe

Thermal leprogenesis in $SO(10)$ (Buchmuller, Plumacher et al)



m_ν too small : Yukawa couplings too small to bring heavy N into equilibrium

m_ν too large : Erasure processes too efficient

$$M_N \gtrsim O(10^9) \text{GeV} \left(\frac{2.5 \times 10^{-3}}{Y_N} \right) \left(\frac{0.05 \text{eV}}{m_\nu} \right)$$

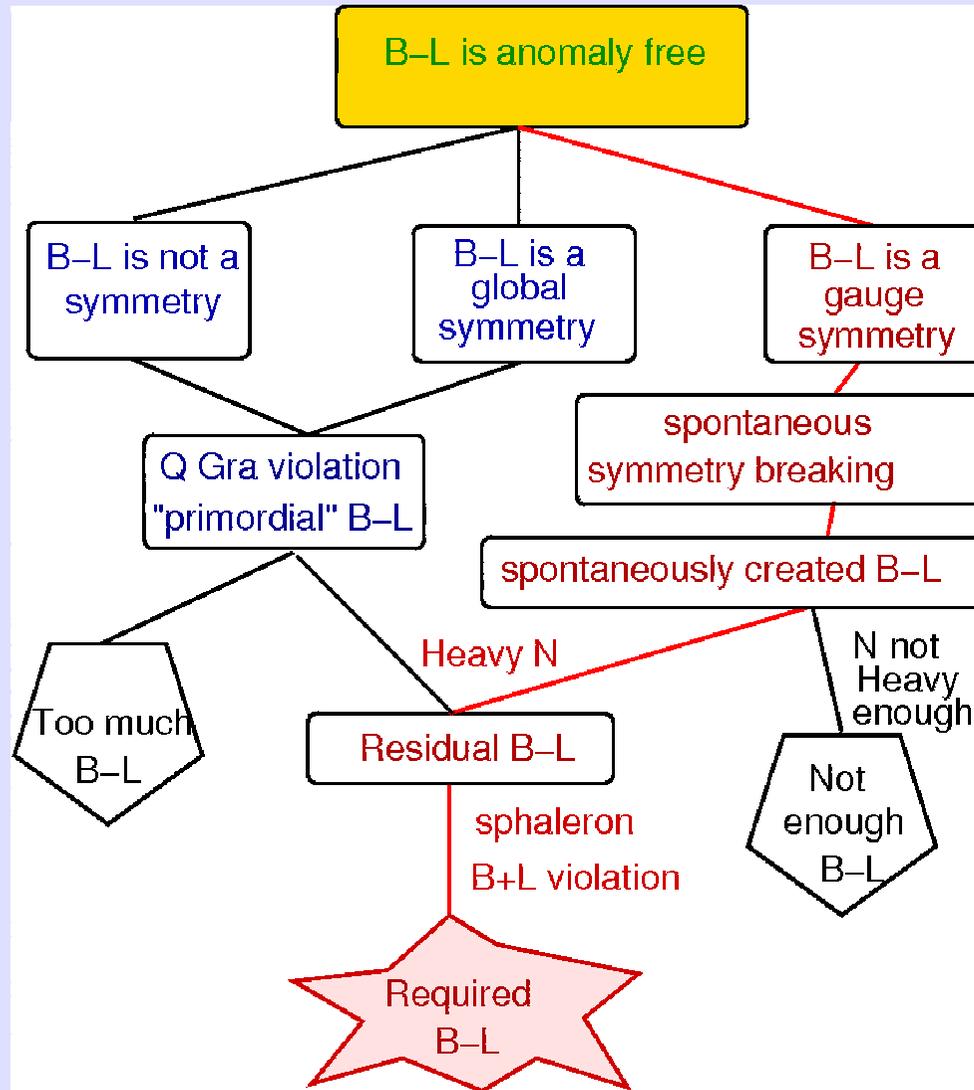
More on Leptogenesis

- $M_N \gtrsim 10^9$ GeV – does not sit well with hierarchy in non-SUSY case
 - Conflicts with Supersymmetric unification \rightarrow gravitino overproduction
- Low energy neutrino mass differences are reasonably well constrained
- Analysis of see-saw formula with three generations taken into account show, for thermal leptogenesis, (Davidson and Ybarra)

$$|\varepsilon_{CP}| \leq 10^{-7} \left(\frac{M_1}{10^9 \text{GeV}} \right) \left(\frac{m_3}{0.05 \text{eV}} \right)$$

- This can be too small for producing the asymmetry

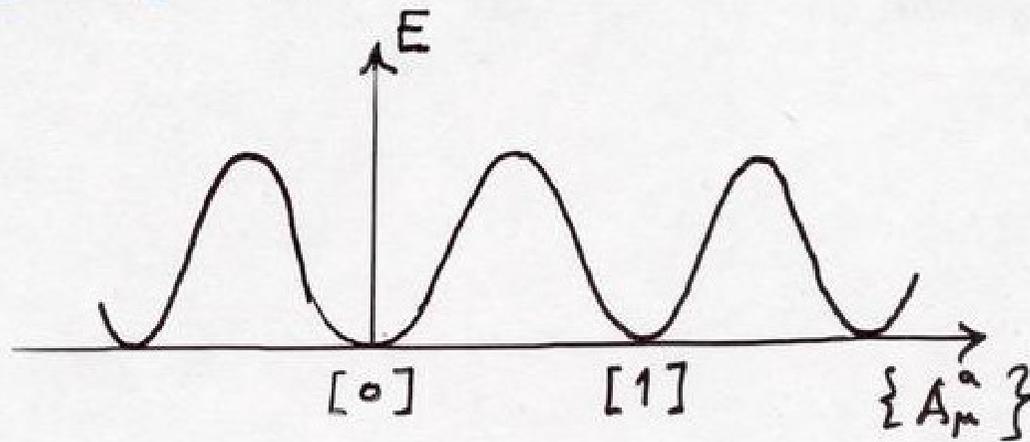
What choices did god have?



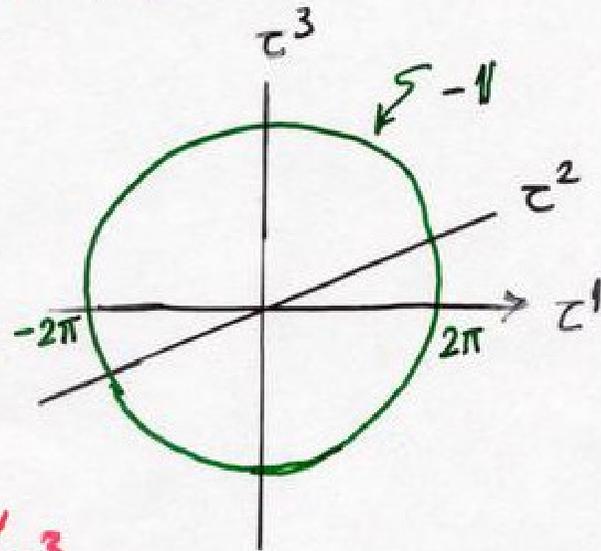
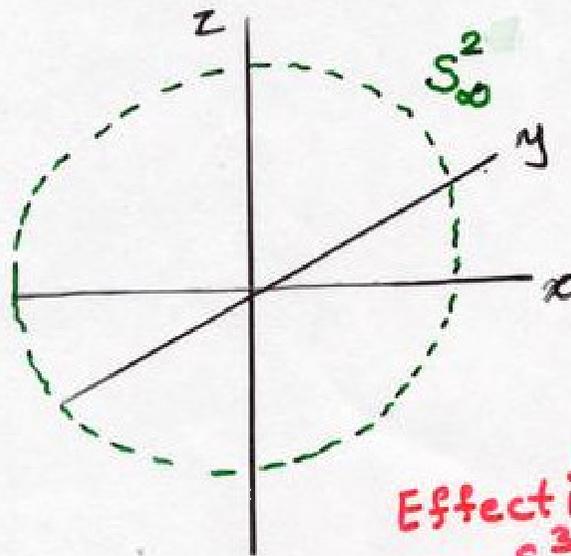
Details of : Anomalous violation of $B + L$

- Gauge theories are non-linear and possess a non-trivial vacuum structure (Jackiw-Rebbi 1973; Klimkhammer-Manton; Soni 1984)

"Large" gauge transformations



$$U_{J-R}^{[1]} = \frac{\lambda^2 - r^2}{\lambda^2 + r^2} + i \frac{2 \vec{e} \cdot \vec{r} \lambda}{\lambda^2 + r^2}$$



Effectively
 $S^3 \rightarrow S^3$

Each vacuum characterised by

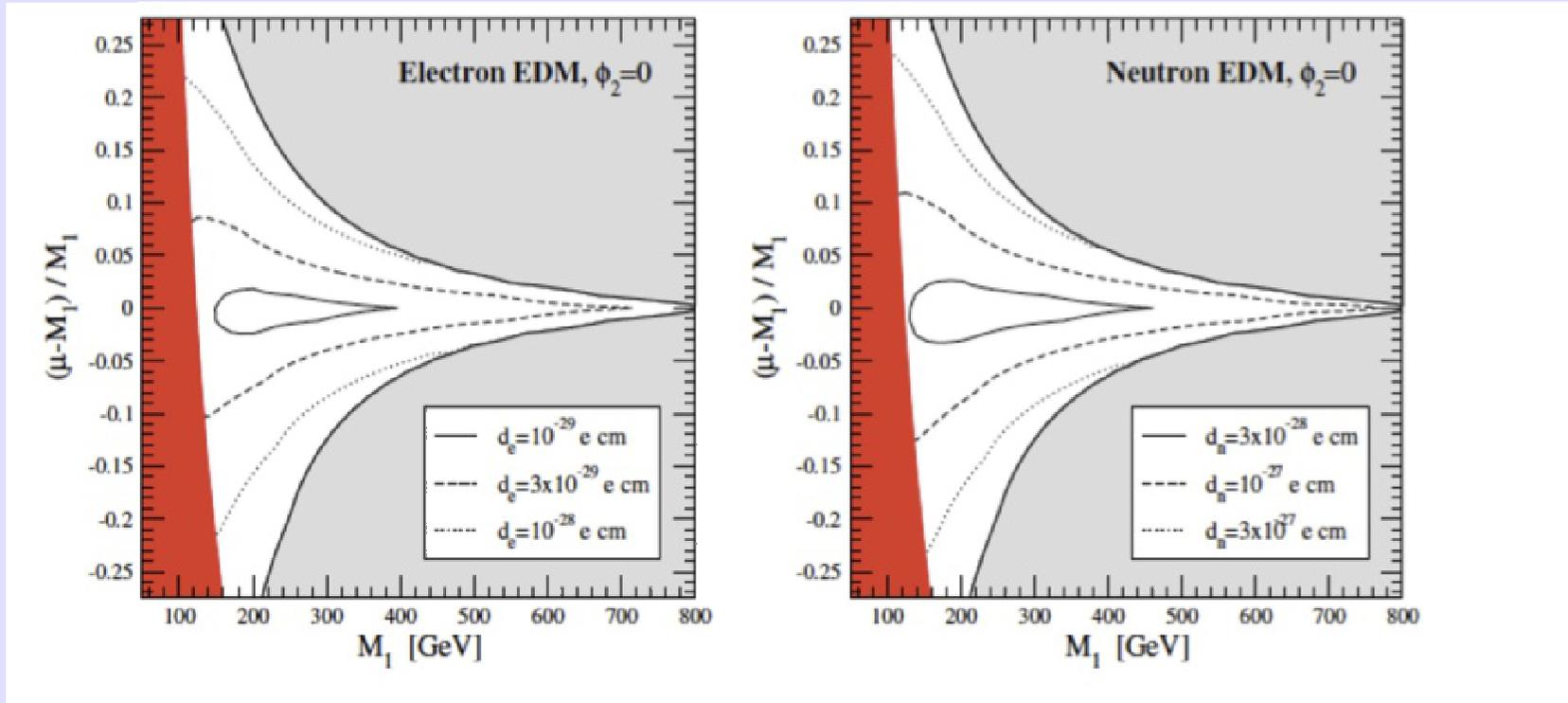
$$N_g = \int d^3x K^0$$

where

$$K^\mu = \text{Tr} \varepsilon^{\mu\nu\rho\sigma} \left(A_\nu \partial_\rho A_\sigma - \frac{2}{3} A_\nu A_\rho A_\sigma \right)$$

Interestingly, if there are chiral fermions coupled to this gauge field, then their axial current turns out to be anomalous in QFT, resulting in

$$\Delta N_F = \Delta N_g$$



Morrissey and Ramsey-Musolf (2012)

$$d_f \cong \sin \delta_{\text{CP}} \left(\frac{m_f}{\text{MeV}} \right) \left(\frac{1 \text{ TeV}}{M} \right)^2 \times 10^{-26} \text{ e cm}$$

With $M \sim 500 \text{ GeV}$ for sufficient abundance at 100 GeV , $\delta_{\text{CP}} \sim 0.01$ and not adequate source of baryon asymmetry from the walls.

SUSY partner becoming heavy (split SUSY) can suppress the one-loop EDM, yet preserve B-generations \rightarrow untestable from EDM.

Neutrino mass and after

How do we accommodate the neutrino mass?

- $M_L \overline{\nu}_L^C \nu_L$ violates the $SU(2)_L$ invariance.
- Higher order operator :

$$\mathcal{L} \sim \frac{c_1}{\Lambda_\nu} \text{Tr} \left(\phi \tilde{\phi}^\dagger l_L l_L^{\bar{C}} \right) \sim \frac{c_1}{\Lambda_\nu} \overline{\nu}_L^C \langle \phi \rangle^2 \nu_L$$

- This means there is a scale $\Lambda_\nu \sim O(10^{15})\text{GeV}$ with some new physics which gives rise to the $m_\nu \sim O(0.1)\text{eV}$
- No new species required but the new scale forced to be GUT

- We have not yet seen any sign of GUT scale
 - generically expect proton decay

“Just” Beyond the SM ?

GUT naturalness of gauge coupling unification; \rightarrow see-saw M_N was expected to fit in.

- \rightarrow It did, provided $m_D \approx 100\text{GeV}$. (Still $M_{\text{GUT}} \sim 10^{16}\text{GeV}$, $M_N \sim 10^{12}\text{GeV}$)
- \rightarrow The only guide to neutrino Dirac mass m_D could be charged fermions mass.
- \rightarrow Unfortunately m_D values for charged fermions are scattered from 175GeV to 1 MeV .
- \rightarrow Unfortunately also, light neutrino mass differences (known since 1998) imply an order of magnitude variation in m_2 values.

Left-right as JBSM

Just Beyond the Standard Model ... $SU(2)_L \otimes SU(2)_R \otimes U(1)_X$

Gauged $B - L$

$$\begin{array}{c}
 \tau_L^3 \quad \tau_R^3 \quad \frac{1}{2}X \quad Q \\
 \left[\begin{array}{c} \nu_L \\ e_L^- \end{array} \right] \left[\begin{array}{cccc} +\frac{1}{2} & 0 & -\frac{1}{2} & 0 \\ -\frac{1}{2} & 0 & -\frac{1}{2} & -1 \end{array} \right] \\
 \left[\begin{array}{c} \nu_R \\ e_R^- \end{array} \right] \left[\begin{array}{cccc} 0 & +\frac{1}{2} & -\frac{1}{2} & 0 \\ 0 & -\frac{1}{2} & -\frac{1}{2} & -1 \end{array} \right] \\
 \\
 \tau_L^3 \quad \tau_R^3 \quad \frac{1}{2}X \quad Q \\
 \left[\begin{array}{c} u_L \\ d_L \end{array} \right] \left[\begin{array}{cccc} +\frac{1}{2} & 0 & +\frac{1}{6} & +\frac{2}{3} \\ -\frac{1}{2} & 0 & +\frac{1}{6} & -\frac{1}{3} \end{array} \right] \\
 \left[\begin{array}{c} u_R \\ d_R \end{array} \right] \left[\begin{array}{cccc} 0 & +\frac{1}{2} & +\frac{1}{6} & +\frac{2}{3} \\ 0 & -\frac{1}{2} & +\frac{1}{6} & -\frac{1}{3} \end{array} \right]
 \end{array}$$

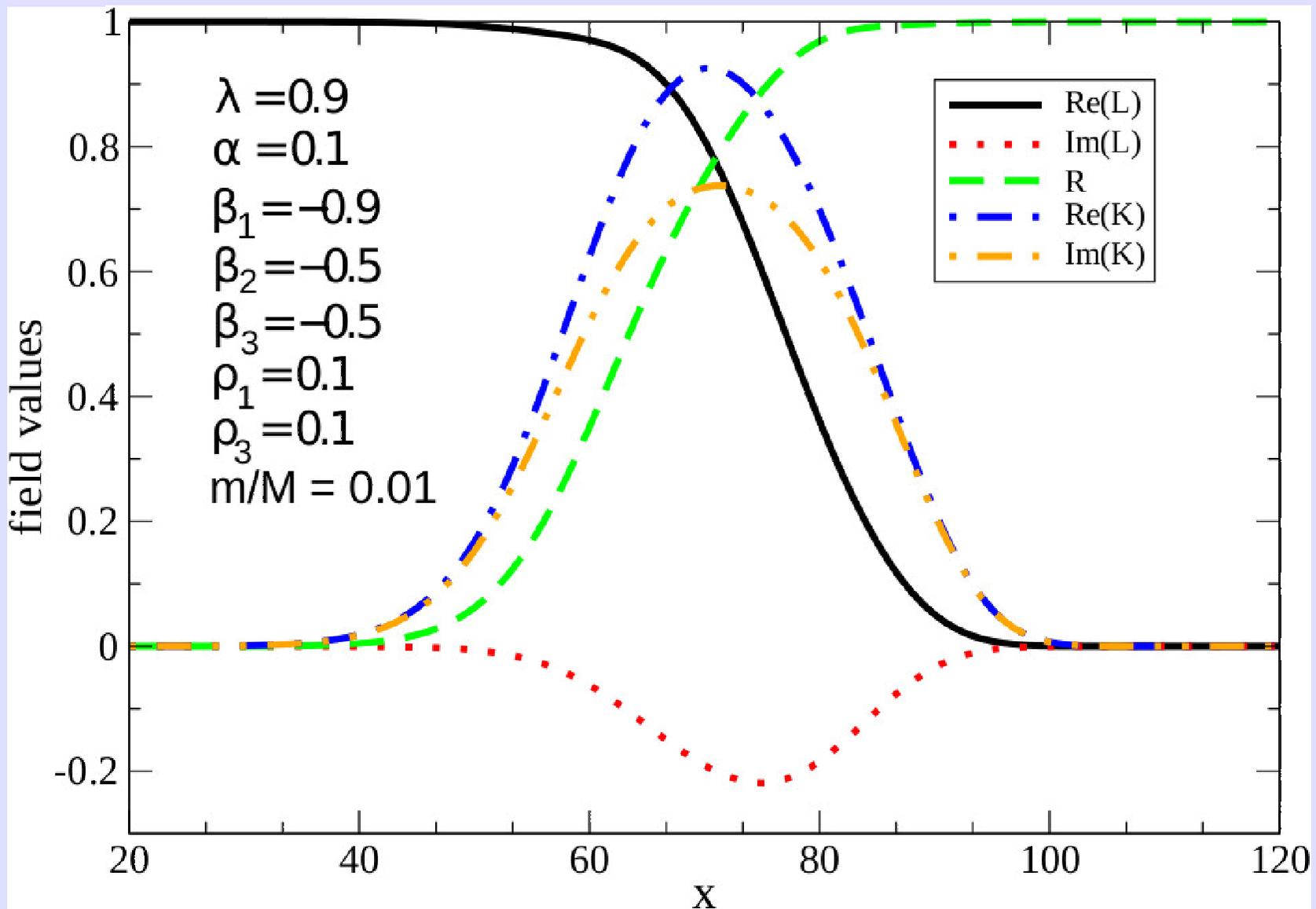
- Introduced new species $\nu_R \rightarrow$ as a partner to e_R^-
- New gauge symmetry $SU(2)_R$
- Need a new hypercharge $X \rightarrow$ turns out to be exactly $B - L$
- In praise of $B - L$... the only conserved charge of SM which is not gauged!
 \rightarrow Hereby it gains the status of being gauged

Non-thermal leptogenesis

If we ask the reverse question : if the N mass is not as high as required for thermal Leptogenesis, do we still have the scope for producing baryon asymmetry?

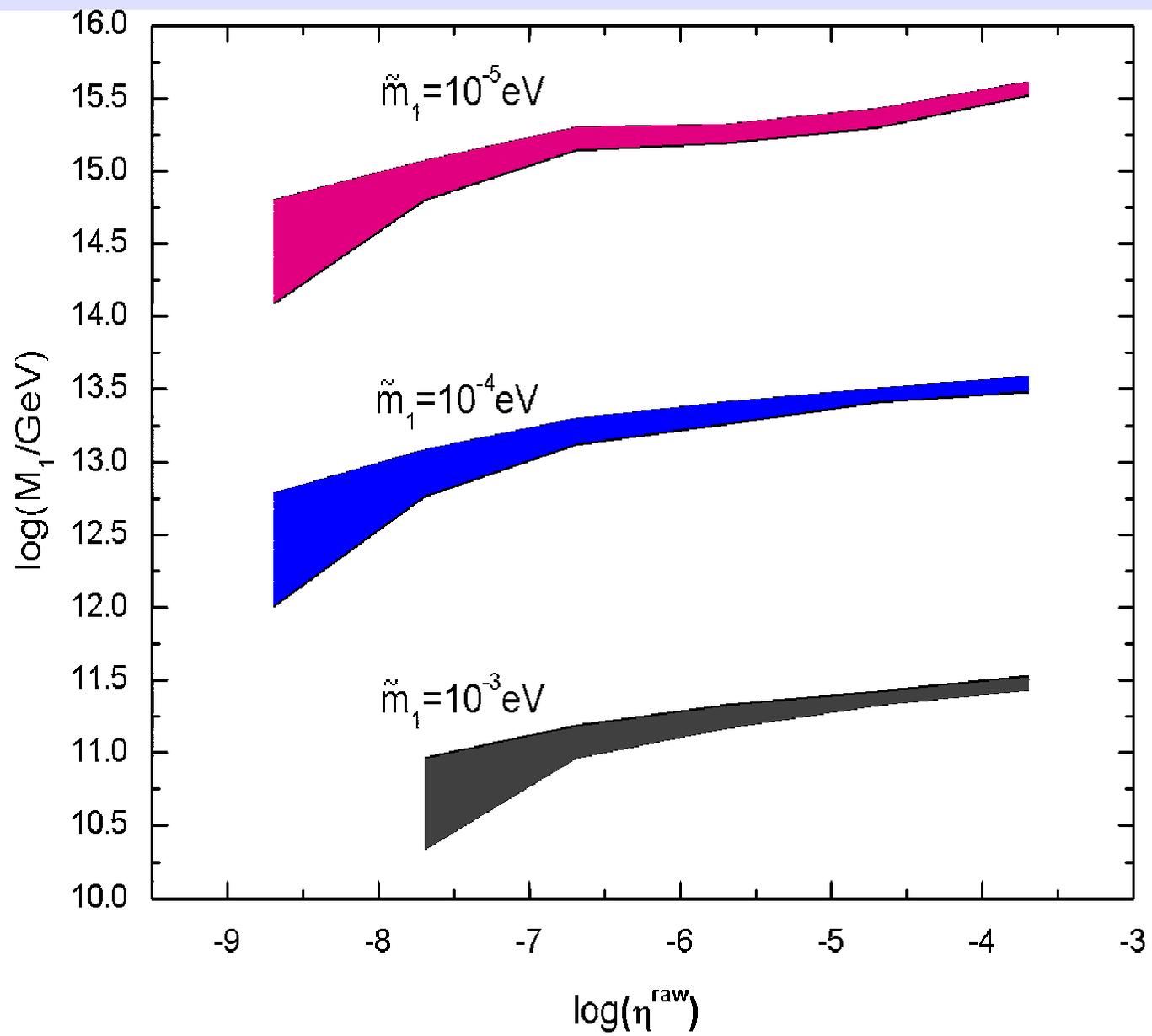
The answer is yes. ([Sarkar, UAY 2003](#))

- The left-right symmetric model has domain walls, with sufficient CP violation provided by the scalar condensates to produce lepton number at a low scale.
- The effect is the same as having bubble walls



Can this lepton asymmetry survive?

This question was answered in the affirmative, solving Boltzmann equations ([Narendra Sahu and UAY 2005](#))



Conclusions and caveats

- Thermal leptogenesis is viable and appealing \rightarrow lives necessarily at high

scale -:(

- Tantalising possibility of accessing this high scale physics through see-saw constraints \rightarrow already making it difficult as an explanation
- MSSM baryogenesis is severely constrained
 - Also unclear whether the CP phase can be ascertained in LHC
- Our recommendation : Believe in **JBSM** Left-Right model
 - UV completion through SUSY / extra dimensions
 - Leptogenesis through L-R domain walls \rightarrow robust conclusion about the nature of phase transition
 - Main problem of JBSM : how to get rid of the domain walls after they did their job. (Narendra Sahu, Anjishnu Sarkar, Sasmita Mishra, Debasish Borah).

THANK YOU