Some Studies in Violation of Symmetry Principles in Particle Physics

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Rishikesh D. Vaidya

Under the Supervision of

Dr. Subhendra Mohanty
Physical Research Laboratory

Theoretical Physics Division
Physical Research Laboratory, Ahmedabad.

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Certificate

CERTIFIED that the work incorporated in the thesis

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submitted by Mr. Rishikesh D. Vaidya, was carried out by the candidate under my guidance at the Physical Research Laboratory, Ahmedabad. The work presented in this thesis is original and has not formed basis for the award of any degree or diploma by any university or institution.

Dr. Subhendra Mohanty
(Supervisor)

To...

...those authors, whose pedagogic books and reviews have immensely influenced my understanding of Physics. The view from the window they provided, was just too beautiful.

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Rishikesh Vaidya
PRL, Ahmedabad.

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For Full text Please Contact

To

rishi@theory.tifr.res.in