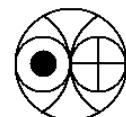


Studies on time dependent and stationary classically chaotic quantum systems

A Thesis submitted to
Gujarat University

for the degree of
Doctor of Philosophy in Physics

by
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November 2001

Certificate

I hereby declare that the work presented in this thesis is original and has not formed the basis for the award of any degree or diploma by any University or Institution.

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dedicated to
my parents

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Contents

1	Introduction	1
1.1	Chaos in Hamiltonian systems	2
1.1.1	Integrable systems	3
1.1.2	Nonintegrable systems	4
1.1.3	Few examples	5
1.2	Quantum chaos	6
1.2.1	Eigenvalues	7
1.2.2	Eigenstates	8
1.2.3	Statistics	9
1.3	Kicked rotor: a paradigm	11
1.3.1	Dynamical localization	11
1.4	Motivation for the thesis	14
1.4.1	An illustration	15
1.4.2	Outline of the thesis	18
2	Classical map	19
2.1	Introduction	19
2.2	Generalized standard map	20
2.3	Transition to chaos	21
2.4	Stability analysis: new approach	24
2.5	Hyperbolic regime	30
2.6	Diffusion	31
2.7	Summary	36
3	Quantum map	39
3.1	Introduction	39
3.2	Matrix form of quantum propagator	40
3.3	Special case: kicked rotor	43
3.4	Quantum resonance	44
3.5	Results	46
3.5.1	Localization and length scales	46
3.5.2	Localization and classical diffusion	49
3.5.3	Measure of quantum chaos	52

3.5.4	Eigenvalues and eigenstates	54
3.6	Summary	60
4	Accelerator modes	62
4.1	Introduction	62
4.2	Classical modes	63
4.3	Quantum modes	67
4.3.1	Gaussian wave packet	68
4.3.2	Quantum effects and correspondence	69
4.4	Summary	73
5	Quantized torus	74
5.1	Introduction	74
5.2	Quantized GSM	75
5.3	Quasienergies	77
5.4	Quasienergy states and phase space	80
5.4.1	Information entropy	80
5.4.2	Coherent-state representation	82
5.5	Level dynamics	85
5.5.1	Level velocities and RMT predictions	86
5.5.2	Correlation of level velocities	91
5.6	Summary	93
Epilogue		95
Bibliography		97
List of Publications		104

For Fulltext Please Contact

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