

Methods for Efficient Population Transfer and Quantum Logic Gates

A THESIS

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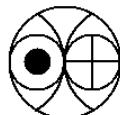
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BY

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CERTIFICATE

I hereby declare that the work presented in this thesis is original and has not formed the basis for the award of any degree or diploma by any University or Institution.

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*to
my parents*

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