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भारत/INDIA
**SOME INVESTIGATIONS IN TIME
DEPENDENT CANONICAL
PERTURBATION THEORY**

thesis submitted to
The Gujarat University
for
THE DEGREE OF DOCTOR OF PHILOSOPHY
in
PHYSICS

by

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