Multiparticle Entanglement and Interference in Cavity Quantum Electrodynamics

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CERTIFICATE

I hereby declare that the work presented in this thesis is original and has not formed the basis for the award of any degree or diploma by any University or institution.

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