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# STUDIES OF LOW FREQUENCY INSTABILITIES IN A COLLISIONLESS PLASMA

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A THESIS
SUBMITTED FOR THE DEGREE OF
DOCTOR OF PHILOSOPHY
OF THE

GUJARAT UNIVERSITY

043

MAY 1975



事的法证明。

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### CERTIFICATE

I hereby declare that the work presented in this thesis is original and has not formed the basis for the award of any degree or diploma by any University or Institution.

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May 15, 1975

## DEDICATED

TO

MY RESPECTED MOTHER

(SMT. DARYAW DEVI)

AND

TO THE SACRED MEMORY OF

MY FATHER

(LATE SRI NEELKANTH VYAS)

#### STATEMENT

The work presented in this thesis is
mainly centred around the study of very low frequency
wave particle interactions in collisionless plasmas
with a view to (i) investigating the generation
mechanism for the magnetospheric VLF emissions, and
(ii) explaining the favourable triggering of these
emissions at half the equatorial gyrofrequency
along the field line of their propagation.

Our approach to this study consists in first finding how the waves affect or modify the plasma particle distribution function and then investigating how this modified distribution affects low amplitude perturbations existing in the system.

The thesis starts with a preliminary introduction to the magnetospheric plasma and presents a brief survey of the work done by various investigators in the field.

The effect of the Landau resonance of whistler mode pulses on the particle distribution function in a homogenous collissionless magnetoplasma

has been discussed in chapter II and an extension of the model for VLF emissions proposed by Das (1968) has been presented in chapter III. The model is based on gyro resonant interaction and the modification made therein is the inclusion of the effect of increasing the amplitude of a resonant pulse beyond a certain critical limit.

Then the question of the preferential triggering of VLF emissions at half the equatorial electron gyrofrequency has been taken up. The behaviour of whistler mode dispersion relation has been examined carefully and it is found that it exhibits many interesting characteristics at that frequency. The influence of these characteristics on the generation of VLF emissions has been investigated in great detail in chapter IV and V and the results have been found to be quite encouraging.

In both the chapters IV and V, the emphasis has been put on the effects of Landau resonance.

The former discusses the Landau resonant diffusion of particles in velocity space and the latter presents a study of the effects of Landau damping

on the gyroresonant interaction.

The last chapter presents a synoptic view of the whole work and gives a discussion of the results obtained. The scope for future work has also been pointed out towards the end of the thesis.

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MAY 15, 1975

#### ACKNOWLEDGMENTS

I wish to express my sincere appreciation to Dr. Anath Chandra Das for his guidance, patience, magnanimity, stimulating counsel and ever helpful attitude during all phases of this work.

I have received enormous help and encouragement from Mr. Ram Rattan in completing this work. I am deeply indebted to him.

I acknowledge the helpful discussions that I used to have quite often with Mr. V.H. Kulkarni, Mr. R.K. Jain and Mr. Y.S. Satya.

My sincere acknowledgements are due to all the plasma physicists and other scientists who worked at the Physical Research Laboratory during the course of this work and helped me in some way or other in getting ahead with the work.

The help of Dr.K.S. Rao and Dr.D.R. Kulkarni in solving computational problems was invaluable. I express my sincere thanks to them. I also acknowledge

the general cooperation of the personnel of the PRL Computer Centre.

I am very much thankful to Dr. Dinesh Patel for his general helpful attitude.

I wish to express my special appreciation to Mr.D.S. Kamat Mr. H.S. Raina and Mr. N.V. Maslekar who consistently encouraged and consoled me in my efforts and often turned despair into renewed hope.

I acknowledge the neat and prompt typing of the manuscript by Mr. P.P. Narayanan.

It is a pleasure to acknowledge the keen interest taken in the progress of this work by all my friends both at the Physical Research Laboratory and in the Indian Space Research Organisation.

I am also grateful to all others who helped me directly or indirectly in bringing this work to the present shape.

Whatever value this work may have, however, may be attributed in large part to my uncles, brothers and cousins who, right from the beginning, helped me in cultivating an interest for learning.

Mand Kishore Vyas
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