First and Second order Coherence Studies of Optical Vortices

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by

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Under the Supervision of

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CERTIFICATE

I feel great pleasure in certifying the thesis entitled "First and Second order Coherence Studies of Optical Vortices" by Mr. Ashok Kumar under my guidance. He has completed the following requirements as per Ph.D. regulations of the University

(a) Course work as per the university rules.

(b) Residential requirements of the university.

(c) Presented his work in the departmental committee.

(d) Published/accepted minimum of two research papers in referred research journals,

I am satisfied with the analysis of data, interpretation of results and conclusions drawn.

I recommend the submission of the thesis.

Date: June 29, 2011

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Countersigned by Head of the Department

DECLARATION

I Ashok Kumar, S/O Shri Dharmanand, resident of C-102, PRL residences, Navrangpura, Ahmedabad - 380009, hereby declare that the research work incorporated in the present thesis entitled "First and Second order Coherence Studies of Optical Vortices" is my own work and is original. This work (in part or in full) has not been submitted to any university or institute for the award of a Degree or a Diploma. I have properly acknowledged the material collected from secondary sources wherever required. I solely own the responsibility for the originality of the entire content.

Date: June 29, 2011

Ashok Kumar (Author)

To my

Parents (Eeja & Pitaji)

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Abstract

Optical vortices, manifestation of phase singularities, are light beams with helical wavefronts. This dissertation concerns with the study of the first and the second order coherences of optical vortices.

We have used computer generated holography technique for the generation of optical vortices. An algorithm has been developed to make a vortex of variable core size and demonstrated experimentally. Interferometric techniques have been described to characterize the optical vortices.

It has been observed that the diffraction of an optical vortex through an iris diaphragm produces ball bearing sort of structures of darkness and brightness. The singularity of the vortex beam is found to be persistent even after diffraction through the aperture. The position of the singularity in the diffracted beam depends on the relative positions of vortex center and the center of iris diaphragm. These results may have implications to sub-diffraction imaging. A further study of diffraction through a two dimensional sinusoidal grating produces four copies of vortex with the same topological charge.

The stability and the propagation dynamics of high topological charge optical vortices have also been discussed. We introduce an asymmetry in the core of a high charge optical vortex by using a spatial light modulator. The splitting of a high charge optical vortex core into unit charge vortices has been found to depend on the extent of introduced asymmetry. The trajectories of the split unit charged vortices and their separation have been recorded as a function of change in the asymmetry of the core.

We have examined the spatial coherence characteristics of the one dimensional projection of optical vortices. The obtained spatial coherence function is found to be the characteristic of the order of the vortex. The knowledge of the spatial coherence is used to extract the information entropy and the Wigner distribution function as well. We have studied intensity correlation function for optical vortices passing through a rotating ground glass (RGG) plate and compared them with that of the TEM₀₀ mode of a He-Ne laser beam passing through the same RGG plate. It has been observed that the intensity correlation curves for the scattered optical vortices decrease much faster than the corresponding curve for a TEM₀₀ mode of the He-Ne laser. We attribute this to the complex phase structure of the optical vortices.

Keywords: Singular optics, Optical vortex, Coherence, Diffraction, Stability of high charge vortex, Computer generated holography.

Contents

Abstract					
List of Figures					
Intr	coduction				
1.1	Singul	ar Optics and Optical Vortices	4		
1.2	First (Order Coherence	8		
1.3	Second	d Order Coherence	10		
Gen	ieratio	n and Characterization of Optical Vortices	17		
2.1	Genera	ation of Optical Vortices	18		
	2.1.1	Computer Generated Holography	18		
		2.1.1.1 Computer Generated Holograms	18		
		2.1.1.2 Spatial Light Modulator	21		
	2.1.2	Astigmatic Mode Converter	26		
	2.1.3	Spiral Phase Plate	26		
2.2	Chara	cterization of Optical Vortices	27		
	2.2.1	Topological Charge	28		
	2.2.2	Orbital Angular Momentum	30		
	2.2.3	Propagation	31		
Diff	raction	n Characteristics of Optical Vortices	34		
3.1	Diffrao	ction of Optical Vortex through an Iris Aperture	35		
	bstra st of Intr 1.1 1.2 1.3 Gen 2.1 2.2 Diff 3.1	st of Figure Introducti 1.1 Singul 1.2 First (1.3 Second Generation 2.1 Genera 2.1.1 2.1.2 2.1.3 2.2 Charac 2.2.1 2.2.1 2.2.2 2.2.3 Diffraction 3.1 Diffrac	st of Figures Introduction 1.1 Singular Optics and Optical Vortices 1.2 First Order Coherence 1.3 Second Order Coherence 1.3 Second Order Coherence Ceneration and Characterization of Optical Vortices 2.1 Generation of Optical Vortices 2.1.1 Computer Generated Holography 2.1.1.2 Spatial Light Modulator 2.1.2 Astigmatic Mode Converter 2.1.3 Spiral Phase Plate 2.2 Characterization of Optical Vortices 2.2.1 Topological Charge 2.2.2 Orbital Angular Momentum 2.2.3 Propagation Diffraction Characteristics of Optical Vortices 3.1 Diffraction of Optical Vortex through an Iris Aperture		

Contents

		3.1.1	Experiment	35	
		3.1.2	Simulation	38	
		3.1.3	Diffraction of an Optical Vortex	40	
		3.1.4	Diffraction of a Gaussian Beam	42	
	3.2	Diffrac	ction of Optical Vortices through a Two Dimensional Sinu-		
		soidal Grating			
		3.2.1	Experiment	44	
		3.2.2	Theoretical Analysis	46	
		3.2.3	Copies of Optical Vortices	51	
		3.2.4	Conclusions	54	
4	Stal	ability and Propagation Dynamics of High Charge Optical Vor-			
	tice	5		55	
	4.1	Introd	uction	56	
	4.2	2 Experiment			
	4.3	Theoretical Background			
	4.4	Effect of Asymmetry to High-Charge Optical Vortices			
		4.4.1	Splitting of a Second Order Optical Vortex	61	
		4.4.2	Trajectories of Split Vortices	63	
		4.4.3	Splitting of Higher Order Optical Vortices	66	
	4.5	Conclu	asion	69	
5	Spa	tial Co	oherence Properties of Optical Vortices	70	
	5.1	Introd	uction	71	
	5.2	Theore	etical Analysis	72	
	5.3	Experiment			
	5.4	Two P	Point Correlation Function of Optical Vortices	75	
		5.4.1	One Dimensional Projection of Two Point Correlation Function	76	
		5.4.2	Degree of Coherence	77	
		5.4.3	Information Entropy	78	

Contents

		5.4.4 Wigner Distribution Function	79		
	5.5	Conclusion	80		
6	Inte	ensity Correlation Properties of Optical Vortices	81		
	6.1	Introduction	82		
	6.2	Experiment	83		
	6.3	Intensity Correlation Function for Optical Vortices and TEM_{00}			
		Mode of He-Ne Laser	85		
	6.4	Scattering of Optical Vortices through Rotating Ground Glass Plate	86		
	6.5	Theoretical Analysis	89		
	6.6	Summary	93		
7	Sun	nmary and Scope for Future Work	94		
Bibliography					
Li	List of Publications 11				