

## Assignment-4

① Prove that  $\cos 6\theta = 32 \cos^6 \theta - 48 \cos^4 \theta + 18 \cos^2 \theta - 1$ .

② Prove that  $\frac{\sin 6\theta}{\cos \theta} = 32 \sin^5 \theta - 32 \sin^3 \theta + 6 \sin \theta$ .

③ Prove that  $\sin 7\theta = 7 \sin \theta - 56 \sin^3 \theta + 112 \sin^5 \theta - 64 \sin^7 \theta$ .

④ Prove that  $\frac{1 + \cos 7\theta}{1 + \cos \theta} = (x^3 - x^2 - 2x + 1)^2$  where  $x = 2 \cos \theta$ .

⑤ Expand  $\cos^8 \theta$  in a series of cosines of multiples of  $\theta$ .

⑥ Prove that  $32 \cos^6 \theta = \cos 6\theta + 6 \cos 4\theta + 15 \cos 2\theta + 10$ .

⑦ Prove that  $2^6 \sin^7 \theta = 35 \sin \theta - 21 \sin 3\theta + 7 \sin 5\theta - \sin 7\theta$ .

⑧ Prove that  $\sin^8 \theta = 2^{-7} [\cos 8\theta - 8 \cos 6\theta + 28 \cos 4\theta - 56 \cos 2\theta + 35]$ .

⑨ Prove that  $32 \sin^4 \theta \cos^2 \theta = \cos 6\theta - 2 \cos 4\theta - \cos 2\theta + 2$ .

⑩ Prove that  $\sin^5 \theta \cos^2 \theta = \frac{1}{64} [\sin 7\theta - 3 \sin 5\theta + \sin 3\theta + 5 \sin \theta]$ .

⑪ Prove that  $2^8 \cos^4 \theta \sin^5 \theta = \sin 9\theta - \sin 7\theta - 4 \sin 5\theta + 4 \sin 3\theta + 6 \sin \theta$ .

G-1	1
G-2	2
G-3	3
G-4	4
G-5	5
G-6	6
G-7	7
G-8	8
G-9	9
G-10	10
G-11	11

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